

# AoPS Algebra 2

Textbook: “Intermediate Algebra”, by Richard Rusczyk and Mathew Crawford, the Art of Problem Solving series, ISBN-13: 978-1-934124-04-8

## Course Introduction:

Algebra 2 covers quadratic equations, conics, polynomials, functions, logarithms, clever factorizations and substitutions, systems of equations, sequences and series, symmetric sums, advanced factoring methods, classical inequalities, functional equations, and more. This course goes beyond what you would find in a typical honors Algebra II curriculum, as it covers topics found in honors Algebra II and Precalculus classes, as well as many topics not found in most other curricula. This is a one-year course and is divided into two parts to be taught in two semesters, Algebra 2A and Algebra 2B.

Algebra 2A covers conics, polynomial division, polynomial roots, factoring multivariable polynomials, sequences and series. Algebra 2B covers identities, induction, inequalities, exponents and logarithms, radicals, special classes of functions, and piecewise defined functions.

This course is intended for high-performing students and will focus on problem solving skills. Students will learn via practicing solving problems in the classroom. Each class will have 3 hours where after being introduced with the new material, students spend the rest of the classroom time practicing the new skills.

## **Who Should Take Algebra 2A:**

Students should have a mastery of basic algebra up through and including quadratic equations before taking this course. Typically this class follows our “Algebra 1B” class. Students who have completed typical Algebra 1 may be ready for this class.

An entrance exam should be taken to evaluate student’s readiness.

## **Who Should Take Algebra 2B:**

Students should have a mastery of basic algebra up through and including polynomials, sequences and series, advanced factoring before taking this course. Typically this class follows our “Algebra 2A” class.

An entrance exam should be taken to evaluate student’s readiness.

## **Requirements for Students Registering for Algebra 2A or Algebra 2B**

In general, students in grade 8 – 10 are eligible to register for either one of Algebra 2 courses. All students interested in take any of these courses should pass the corresponding evaluation test.

The test must be taken and submitted before the specified deadline posted by the school web site. The tests are posted on the school web site as well. Please check the class schedule at the school web site.

### **Teaching Plan**

<b>Algebra 2A</b>	
Lesson 1	Ch 5. Conics 5.1 Parabolas 5.2 Problem Solving With Parabolas 5.3 Maxima and Minima of Quadratics
Lesson 2	5.4 Circles 5.5 Ellipses 5.6 Hyperbolas 5.7 Summary
Lesson 3	Ch 6. Polynomial Division 6.1 Polynomial Review 6.2 Introduction to Polynomial Division
Lesson 4	6.3 Synthetic Division 6.4 The Remainder Theorem 6.5 Summary
Lesson 5	Ch 7. Polynomial Roots, Part 1 7.1 The Factor Theorem 7.2 Integer Roots
Lesson 6	7.3 Rational Roots 7.4 Bound
Lesson 7	7.5 Graphing and Fundamental Theorem of Algebra 7.6 Algebraic Applications of the Fundamental Theorem 7.7 Summary
Lesson 8	Ch 8. Polynomial Roots, Part 2 8.1 Irrational Roots 8.2 Nonreal Roots
Lesson 9	8.3 Vieta's Formulae 8.4 Using Roots to Make Equations 8.5 Summary
Lesson 10	Ch 9. Factoring Multivariable Polynomial 9.1 Grouping 9.2 Sums and Differences of Powers
Lesson 11	9.3 The Factor Theorem of Multivariable Polynomial 9.4 Summary
Lesson 12	Ch 10. Sequences and Series 10.1 Arithmetic Sequences 10.2 Arithmetic Series
Lesson 13	10.3 Geometric Sequences 10.4 Geometric Series
Lesson 14	10.5 Sequence, Summation, and Product Notation

	10.6 Nested Sums and Products 10.7 Summary
Lesson 15	Ch 11. Identities, Manipulations, and Induction 11.1 Brute Force 11.2 Ratios
Lesson 16	11.3 Induction 11.4 Binomial Theorem 11.5 Summary

<b>Algebra 2B</b>	
Lesson 1	Ch 11. Identities, Manipulations, and Induction 11.1 Brute Force 11.2 Ratios
Lesson 2	11.3 Induction 11.4 Binomial Theorem 11.5 Summary
Lesson 3	Ch 12. Inequalities 12.1 Manipulating Inequalities 12.2 The Trivial Inequality
Lesson 4	12.3 AM-GM Inequality with Two Variables 12.4 AM-GM Inequality with More Variables
Lesson 5	12.5 The Cauchy-Schwarz Inequality 12.6 Maxima and Minima 12.7 Summary
Lesson 6	Ch 13. Exponents and Logarithms 13.1 Exponential Function Basics 13.2 Introduction to Logarithms
Lesson 7	13.3 Logarithmic Identity 13.4 Using Logarithm Identity
Lesson 8	13.5 Switching Between Loga and Exponents 13.6 Natural Logarithm and Exponential Decay 13.7 Summary
Lesson 9	Ch 14. Radicals 14.1 Raising Radicals to Powers 14.2 Evaluating Expressions with Radicals
Lesson 10	14.3 Radical Conjugates 14.4 Summary
Lesson 11	Ch 15. Special Classes of Functions 15.1 Rational Functions and Their Graphs 15.2 Rational Function Equations and Inequalities
Lesson 12	15.3 Even and Odd Functions 15.4 Monotonic Functions 15.5 Summary
Lesson 13	Ch 16. Piecewise Defined Functions 16.1 Introduction to Piecewise Defined Functions

	16.2 Absolute Value
Lesson 14	16.3 Graphing Absolute Value 16.4 Floor and Ceiling
Lesson 15	16.5 Problem Solving with the Floor Functions 16.6 Summary
Lesson 16	