## NCLS Math 7 Homework, 4/22/2012 Name:

$\qquad$
Arithmetic Sequence

1. Consider the arithmetic sequence $1,4,7,10,13, \ldots$
(a) Find the $15^{\text {th }}$ term in the sequence
(b) Find a formula for the $\mathrm{n}^{\text {th }}$ term in the sequence.
2. The $3^{\text {rd }}$ term of an arithmetic sequence is 5 and the $6^{\text {th }}$ is -1 . Find the $12^{\text {th }}$ term of this sequence.
3. How many terms are in the arithmetic sequence $5,11,17, \ldots, 89$ ?
4. When the $171^{\text {st }}$ even positive integer is subtracted from the $219^{\text {th }}$ odd positive integer, the result is $z$. Find $z$.
5. In the infinite arithmetic sequence $a_{1}, a_{2}, a_{3}, \ldots$, we have $a_{8}=2001$. If the common difference $d$ is an integer, find the minimum value of $d$ so that $a_{17}>10000$.
6. Given an infinite arithmetic sequence $a_{1}, a_{2}, a_{3}, \ldots$, first term is $a_{1}$, common difference is $d$.
(a) If we remove the first $m$ terms and make a new sequence with the remaining terms. Is the new sequence an arithmetic one? If so, what are the values for its first term and common difference?
(b) If we remove all the odd-number terms and make a new sequence with the remaining terms. Is the new sequence an arithmetic one? If so, what are the values for its first term and common difference?
7. Given an arithmetic sequence $\left\{a_{n}\right\}$.
(a) Is it true that $2 a_{5}=a_{3}+a_{7}$ ? $2 a_{5}=a_{1}+a_{9}$ ? Why?
(b) $2 a_{n}=a_{n-1}+a_{n+1}(n>1) ? 2 a_{n}=a_{n-k}+a_{n+k}(n>k>1)$ ?
8. Given an arithmetic sequence $\left\{a_{n}\right\}$, fill in the blank below:

| $a_{1}$ | $A_{3}$ | $A_{5}$ | $A_{7}$ | $d$ |
| :--- | :--- | :--- | :--- | :--- |
| -7 |  | 8 |  |  |
|  | 2 |  |  | -6.5 |

9. A stadium's seating is arranged as follows: the first row has 15 seats. Starting from the second row, every row has two more seats than the previous row. Can you represent $\mathrm{n}^{\text {th }}$ row? How many people can $10^{\text {th }}$ row sit?
10. Under normal condition, between the ground and 10 km sky, whenever the height increases by 1 km , the temperature will drop a fixed value. If the temperature at 1 km is 8.5 C , and at 5 km is 17.5 C . What are the temperatures at $2 \mathrm{~km}, 4 \mathrm{~km}$, and 8 km ?
