## NCLS Math 7 Homework, 5/13/2012 Name:

$\qquad$
Geometric Series

1. Compute the sum of each of the following geometric series:
(a) $-1-3-9-27-81-243-729$
(b) $3-6+12-24+48-\ldots+768$
(c) $100+10+1+0.1+0.01+\ldots$
(d) $8-6+9 / 2-27 / 8+\ldots$
2. Find a simple expression equal to $1+2+2^{2}+2^{3}+2^{4}+\ldots 2^{n}$
3. In each part below, find the fraction that is equal to the given decimal.
(a) $0 . \overline{4}$
(b) $0 . \overline{273}$
(c) $0.63 \overline{5}$
(d) $0.8 \overline{81}$
4. Each term in the sequence $a_{1}=1, a_{2}=0.2, a_{3}=0.04, a_{4}=0.008, \ldots$ is obtained by doubling the previous term of then shifting the decimal point one place to the left. What is the sum of all the term sin the sequence?
5. Find all values of $x$ that satify $x=1-x+x^{2}-x^{3}+x^{4}-x^{5}+\cdots$
6. For each geometric sequence below, find the sum of the first $n$ terms:
(a) $a_{1}=3, r=2, n=6$
(b) $a_{1}=-.27, r=-1 / 3, a_{n}=1 / 90$
7. For a geometric sequence, the sum of first 5 terms is 10 , the sum of 10 terms is 50 , what is the sum of the first 15 terms?
8. $\left\{a_{n}\right\}$ is a geometric sequence, $S_{n}$ is the sum of its first $n$ terms. Prove that $S_{7}, S_{14}-S_{7}, S_{21}-S_{14}$ is also a geometric sequence.
9. $\left\{a_{n}\right\}$ is a geometric sequence, $S_{n}$ is the sum of its first $n$ terms, and $S_{3}, S_{9}, S_{6}$ form an arithmetic sequence. Prove that $a_{2}, a_{8}, a_{5}$ is also an arithmetic sequence.
